

## Rational Functions 2a - Adding & Subtracting with Like Denominators

Standards:A-APR.7, A-SSE.1a

GLO: #3 Complex Thinker

Math Practice: #7 - Look for & make use of Structure

Learning Target

How do you add & subtract rational functions?

**Review:**

Simplify:  $\frac{3}{5} + \frac{1}{5} \rightarrow \frac{3+1}{5} \rightarrow \frac{4}{5}$

To add/subtract rational expressions, they need to have **same denominators.**

(erase to show)

Once they have the same denominator, just add or subtract the numerators and put it over the common denominator.

State the excluded values (i.e. values of  $x$  for which the expression is not defined), then perform the indicated operation.

Operation:

Rational Expression:

Excluded Value:

Add or  
Subtract

$$\frac{3}{2x} - \frac{7}{2x} =$$

$$\frac{\cancel{2}x \neq 0}{\cancel{2} \quad 2}$$

$$\frac{3-7}{2x} \rightarrow \frac{-\cancel{4}2}{\cancel{1}2x} \rightarrow \left( -\frac{2}{x} \right)$$

$$x \neq 0$$

Answer

$$-\frac{2}{x}; x \neq 0$$

$$\frac{2x+5}{x+3} + \frac{-7}{x+3}$$

$$x+3 \neq 0$$

$$\frac{-\cancel{3} \quad -3}{\cancel{3} \quad -3}$$

$$\frac{2x+5-7}{x+3} \rightarrow \frac{2x-2}{x+3}$$

$$x \neq -3$$

$$\frac{2(x-1)}{(x+3)}$$

Answer

$$\frac{2(x-1)}{x+3}; x \neq -3$$

Operation:                      Rational Expression:                      Excluded Value:

Add or                       $\frac{-x+8}{x^2+6x-7} - \frac{-2x+1}{x^2+6x-7}$                        $x^2+6x-7 \neq 0$   
 Subtract

$$\frac{(-x+8) - (-2x+1)}{x^2+6x-7}$$

$$\frac{-x+8+2x-1}{x^2+6x-7}$$

$$\frac{x+7}{x^2+6x-7}$$

$$\frac{\cancel{(x+7)}}{\cancel{(x+7)}(x-1)}$$

$$\boxed{\frac{1}{(x-1)}}$$

$$(x+7)(x-1) \neq 0$$

$$x+7 \neq 0 \quad x-1 \neq 0$$

$$x \neq -7 \quad x \neq 1$$

$$\boxed{x \neq -7, 1}$$

Answer

$$\frac{1}{x-1}; x \neq -7, 1$$

<u>Operation:</u>	<u>Rational Expression:</u>	<u>Excluded Value:</u>
Add or Subtract	$\frac{p^2 - 5p - 21}{5p^2 + 20p + 15} + \frac{6p + 15}{5p^2 + 20p + 15}$	
	$\frac{p^2 - 5p - 21 + 6p + 15}{5p^2 + 20p + 15}$	$5p^2 + 20p + 15 \neq 0$
	$\frac{p^2 + p - 6}{5p^2 + 20p + 15}$	$5(p^2 + 4p + 3) \neq 0$
	$\frac{(p+3)(p-2)}{5(p^2 + 4p + 3)}$	$5(p+3)(p+1) \neq 0$
	$\frac{\cancel{(p+3)}(p-2)}{5\cancel{(p+3)}(p+1)}$	<del><math>5 \neq 0</math></del> $p+3 \neq 0$ $p+1 \neq 0$
	$\frac{(p-2)}{5(p+1)}$	$\boxed{p \neq -3, -1}$
	$\frac{(p-2)}{5(p+1)}$	$\boxed{p \neq -3, -1}$
	<b>Answer</b> $\frac{p-2}{5(p+1)}; p \neq -3, -1$	

Operation:                      Rational Expression:                      Excluded Value:

Add or Subtract       $\frac{10n^2 + 30n + 13}{30n + 36} - \frac{5n^2 + 9n - 5}{30n + 36}$

$$\frac{(10n^2 + 30n + 13) - (5n^2 + 9n - 5)}{30n + 36}$$

$$30n + 36$$

$$\frac{10n^2 + 30n + 13 - 5n^2 - 9n + 5}{30n + 36}$$

$$30n + 36$$

$$\frac{5n^2 + 21n + 18}{30n + 36}$$

$$\frac{\cancel{5n+6}(n+3)}{\cancel{6(5n+6)}}$$

$$\boxed{\frac{(n+3)}{6}}$$

$$30n + 36 \neq 0$$

$$6(5n + 6) \neq 0$$

$$\cancel{6 \neq 0} \quad 5n + 6 \neq 0$$

$$5n \neq -6$$

$$\boxed{n \neq -\frac{6}{5}}$$

Answer

$$\frac{n+3}{6}; n \neq -\frac{6}{5}$$